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Faculty of Mathematics and Computer Science
Department: Computer Science

Delia-Monica DUCA-ILIESCU

COMPUTATIONAL METHODS FOR CHESS

SUMMARY

Scientific supervisor

Prof. Dr. Marius-Sabin TĂBÎRCĂ

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Acknowledgements

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Research Motivation

In recent decades, computer-based strategic games have contributed to a deeper understanding of how both humans and computers make decisions under conditions of uncertainty. They have represented a fertile ground for the development of computational methods and software applications. Moreover, strategic games and advances in computational methods have exhibited a relationship of mutual influence ([26], [53]). In this context, chess has become a classical example of a domain in which decision-making complexity continuously interacts with computational methods. Why uncertainty in the case of chess? Although chess is a game of perfect information, in which both players have access to the same board configuration and the same information throughout the entire game, the number of possible moves is estimated to exceed 10^{120} [78]. Furthermore, the possibility of repeating positions through moves that return to previous configurations creates an infinite number of options, making a complete evaluation of all possible variations infeasible. Even with substantial computational resources, such as those employed by programs developed by DeepMind [74], uncertainty remains inevitable, and determining the optimal move continues to represent an ongoing challenge.

This doctoral work was approached with equal passion for computer science and chess, seeking to highlight the reciprocal influence of technology within the field of strategic games, with a particular emphasis on chess. The evolution and diversification of computational methods applied to chess were analyzed, along with the educational value of chess, the various types of notation used in the game, and the automatic recognition of pieces on the chessboard.

Over the years, chess has served as a testing ground for various computational methods that were later applied in other domains [58]. The present research aims to explore the use of computational methods for the evaluation of chess diagrams and their automatic composition.

A composed chess diagram is considered valuable if it possesses specific attributes that are taken into account by nearly every member of a chess jury involved in the composition and solving of chess problems. Certain computational approaches have been attempted in the past; however, they did not lead to practical results suitable for inclusion in the daily judging of chess diagrams ([82], [20]).

The ultimate goal of this thesis is to develop a system capable of automatically composing chess diagrams, which will also be used to evaluate and optimize the generated diagrams. Subsequently, a chess book containing the most remarkable automatically generated diagrams, together with their solutions, could be published.

Personal Contributions

Within the doctoral work to which this summary refers, particular attention was devoted to the automatic composition of chess diagrams, with a specific focus on two-move checkmate problems. Based on the system developed for generating chess diagrams, the subsequent step of the research consisted in exploring the possibility of automatically evaluating such diagrams. Metrics were defined in order to determine the degree of beauty of an already composed or automatically generated diagram. A valuable chess problem is one that possesses multiple qualities, such as, for example, material economy or a subtle key move for the verification of the mentioned criteria). Another criterion for diagrams in which White moves and delivers checkmate in n moves is related to the defensive variations and does not consist solely in the number of defensive responses available to Black, but also in the uniqueness of White's mate against each of these defenses. These criteria make the diagram more highly appreciated by jury members, as well as by solvers. Furthermore, it is desirable for a diagram to contain a theme or an element that creates a distinctive artistic impression. For instance, if the apparent play¹ includes the moves $a-b$ and each of these moves leads to the mate $c-d$, and in the solution there exists a key move X that changes the order of Black's defenses and leads to the mate $d-c$, a pleasing artistic impression is thus created.

The idea of automatically composing chess diagrams remains largely unexplored. A recent example is the article [50], in which so-called "puzzle" positions² are generated using genetic algorithms and the Stockfish engine. The generated positions cannot be regarded as compositions, since they fail to satisfy, among other criteria, legal constraints related to the pieces, such as the maximum number of pawns per color. In the model proposed in what follows, these constraints are implicitly enforced already at the diagram composition interface, which guarantees the structural validity of each position. Moreover, the approach described in [50] does not implement evaluation criteria for diagrams and does not pursue aesthetic or thematic optimization, as Stockfish is used solely to verify the existence of a checkmate within a specified number of moves.

A methodology for the composition and evaluation of chess diagrams based on a list of criteria was proposed, and a system for optimizing the generated diagrams was developed. The proposed methodology may have multiple practical applications, such as judging chess composition competitions, selecting diagrams for publication, or developing databases (which may lead to the publication of books) containing automatically generated chess diagrams, classified and evaluated according to multiple criteria.

The ideas presented in this work were disseminated at several CORE-listed and indexed conferences, such as the International Conference on Information and Software Technologies (ICIST) and the Advanced Information Networking and Applications Conference (AINA, CORE B listed). In addition, several articles were published in journals indexed by Web of Science (WOS), including one single-author publication [21].

¹Apparent play refers to what would occur on the board if Black were to move in the initial position of the composition, although in reality the move belongs to White. It is frequently used to highlight thematic ideas, such as White's responses to various Black moves, and serves as a contrast or prefiguration of the actual play that follows after the key move of the problem.

²The term "puzzle" in the context of chess refers to positions similar to those arising in practical chess games, analyzed with the purpose of tactical solving, often containing many superfluous pieces, as opposed to chess diagrams that must comply with strict rules and aesthetic criteria in order to be considered artistic compositions.

Papers published in journals with impact factor

1) Publication as sole author of an ISI-indexed article:

“The Impact of Artificial Intelligence on the Chess World”[21]

Author: DM Duca Iliescu

Journal: JMIR Serious Games – Impact factor 3.8

WOS No.: 000632268800010

<https://www.webofscience.com/wos/woscc/full-record/WOS:000632268800010>

<https://www.doi.org/10.2196/24049>

2) Co-author of an ISI-indexed article:

“Personal Health Metrics Data Management Using Symmetric 5G Data Channels”[13]

Authors: R Bocu, A Vasilescu, DM Duca Iliescu

Journal: Symmetry-Basel, Impact factor 2.2

WOS No.: 000831607000001

<https://www.webofscience.com/wos/woscc/full-record/WOS:000831607000001>

<https://www.doi.org/10.3390/sym14071387>

Papers presented at indexed conferences

1) Paper presented at the Scopus-listed Conference “International Conference on Information and Software Technologies” (ICIST) 2024, with the paper subsequently published by Springer: “Efficient Didactic Methods Used in Modern E-Learning and Traditional Environments”

Authors: Constantin Lucian Aldea, Razvan Bocu, Delia Monica Duca Iliescu, Anca Vasilescu

<https://www.webofscience.com/wos/woscc/full-record/WOS:001481366300022>

https://www.doi.org/10.1007/978-3-031-84263-4_22

Springer link: https://link.springer.com/chapter/10.1007/978-3-031-84263-4_22 [5].

2) Paper presented at the Core-listed Conference (category B) “Advanced Information Networking and Applications Conference” (AINA), 2024 – with the paper subsequently published by Springer: “Health Parameters Monitoring Through an Integrated Multilayer Digital Twin Architecture”

Authors: Constantin Lucian Aldea, Razvan Bocu, Delia Monica Duca Iliescu

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<https://www.webofscience.com/wos/woscc/full-record/WOS:001264727500027>

https://www.doi.org/10.1007/978-3-031-57840-3_27

Springer link: https://link.springer.com/chapter/10.1007/978-3-031-57840-3_27

3) Paper presented at the Scopus-listed Conference “Elearning and Software for Education” (eLSE) 2023 with the paper “Applied Research Concerning the Aspects and Methods Used in Modern Learning Environments”

Authors: Constantin Lucian Aldea, Razvan Bocu, Delia Monica Duca Iliescu, Anca Vasilescu

<https://www.scopus.com/pages/publications/85219122571>

4) Invited speaker at the Core-listed Conference (category C) “Conference on Games” (CoG), 2022 – with the paper: “The Impact of Artificial Intelligence on the Chess World”

Author: Delia Monica Duca Iliescu

Conference program: <https://ieee-cog.org/2022/ProgramOfCoG2022-Formal.pdf> (pp.37)

Accepted paper

1) Constantin Lucian Aldea, Razvan Bocu, Delia Monica Duca Iliescu. “On the analysis and prediction of chess diagram scores using artificial neural networks”. In: The 40-th International Conference on Advanced Information Networking and Applications 2026 – Section Intelligent Computing and Machine Learning (AINA, 2026). <https://voyager.ce.fit.ac.jp/conf/aina/2026/program> [4]

Other conference and workshop participations

1) Invited speaker at the TEDx "Simplicity. Less is More" Conference, Braşov, 2025
<https://youtu.be/TtY0AISJDLI>

2) Poster presentation “Magne 2D Chess Scan” at the “AFCO” Conference organized by Transilvania University of Braşov, 2022
https://afco.unitbv.ro/2022/images/Documente/Lucrarile_AFCO_2022.pdf

3) Invited speaker at the “Artificial Intelligence meets Big Data” Conference, London, 2021
<https://chessconference.org/sunday-6th-dec/>

4) Invited speaker at the “London Chess Conference” – joint session with the authors of the AlphaZero algorithm and presentation of the individual chess study board in 2D format, London, 2020
<https://youtu.be/wvgSqN6M9L8>

5) Workshop attendance at “Machine Learning and Applications Summer School” (MLASS), Braşov, 2019
<https://www.unitbv.ro/cercetare/evenimente/3148-mlass-2019.html>

6) Invited speaker at the BookLand Evolution Conferences, Braşov, 2019
<https://youtu.be/AXrBIFmmy2M>

7) Presentation at the “MACOS” Conference (organized by Transilvania University of Braşov) with the paper “Search Optimization in Chess”, Braşov, 2018
<https://mateinfo.unitbv.ro/en/macros/macros-2018.html>

Thesis Structure

The structure of the doctoral thesis referred to in this summary is as follows:

Chapter 1 - Introduction

The introductory chapter presents the motivations underlying the initiation of this research, together with an overview of the published articles and participation in relevant conferences and workshops. Furthermore, the main personal contributions of this work are briefly highlighted, as well as the overall structure of the thesis.

Chapter 2 - Related research in the scientific literature

This chapter explores relevant research from the scientific literature in the field of strategic games. In addition, existing studies on the educational value of strategic games are presented, with a particular focus on chess, highlighting their impact on cognitive development and strategic thinking skills. Studies and works addressing similar aspects or related topics are examined, emphasizing the research opportunities that are addressed in this thesis.

Chapter 3 - The impact of computational evolution in the world of chess

Chapter 3 analyzes the fundamental concepts underlying strategic games. In addition, the evolution and diversification of computational methods used in the context of chess are investigated, as well as possible directions for technological development in the context of strategic games. New methods for automatic recognition of the chessboard are also explored, and the conversion between different types of chess notation is analyzed using the Magne 2D App.

Chapter 4 - Proposed directions for chess diagram generation

Chapter 4 defines criteria for the evaluation of chess diagrams, describes the concept of automatic generation of a chess diagram book, and proposes a methodology for the automatic composition and evaluation of chess diagrams.

Chapter 5 - Conclusions

Chapter 5 presents a series of conclusions regarding the impact of technology on the world of chess, new directions, and the methodologies proposed in this work.

The final objective was to propose a system for the composition and evaluation of chess diagrams. Thus, the intention was to bring significant contributions to the field of chess composition. The development of a system capable of automatically generating chess diagrams and evaluating them using a set of characteristics represents an important step in the field of chess composition. The system can be used both to create new chess diagrams and to evaluate existing ones. After a chess diagram has been generated, the system uses a set of features to evaluate its aesthetic quality. The evaluation can be performed by the system in real time, providing immediate feedback on the quality of the generated chess diagram, and, ultimately, the diagram can be optimized.

Summary of the Research on the Evaluation of Chess Diagrams Presented in the Thesis

The main objective of the research was to develop a methodology for evaluating chess diagrams based on a set of multiple “beauty” criteria, as well as to explore the possibility of automatically generating and optimizing chess compositions.

The first study presented in the thesis is that of Dobrescu [20], who proposed an evaluation model based on static criteria (material size, piece arrangement, balance of forces, initial level of tension) and dynamic criteria (an unconventional key move, its strategic impact, and aesthetic quality). Subsequently, the author introduced additional criteria such as the depth of variations and the difficulty of finding the solution, which added a new dimension to the aesthetic evaluation of chess problems.

Iqbal [49] continued research in this field by focusing on the concept of economy in chess compositions and proposing a computational function capable of distinguishing economic differences between positions. The results confirm that the evaluation of compositions can be formalized and translated into an algorithmic framework.

Building on these contributions, in Section 4.5 of the thesis I proposed a methodology designed to integrate multiple criteria: from material economy to the symmetry of defensive variations [82], adherence to established themes [85], and the uniqueness and diversity of mates. These criteria reflect both the objective dimension of evaluation (positional balance) and the aesthetic and creative dimension of compositions.

Specialized literature confirms that a composed chess problem is considered a genuine artistic creation that must meet strict requirements. Ianovic [47] emphasizes the need to respect principles such as maximum material economy, uniqueness of the solution, subtlety of the key move, and diversity of Black’s defenses. Similarly, Toth [83] highlights the importance of including well-established compositional themes, which give identity and artistic value to a diagram.

Beyond traditional analysis, recent research also addresses the potential of artificial intelligence in relation to creativity. Grassini [38] compared the generative flexibility of ChatGPT-4 with human creativity, finding that although artificial intelligence can produce diverse and innovative interpretations, the subjectively perceived creativity of humans remains superior. Watkins [86] reinforces this observation, arguing that artificial intelligence can broaden the scope of possible ideas, but expressiveness and artistic depth remain primarily human attributes.

In conclusion, the evaluation of chess diagrams is an interdisciplinary field situated at the intersection of sport, science, and art. While practical play has already been transformed by algorithms such as AlphaZero and MuZero, artistic composition remains an area in which human intuition and creativity retain a significant advantage. Nevertheless, through the proposed methodologies and recent advances in artificial intelligence, the possibility emerges—perhaps for the first time—that computers may learn aesthetic criteria and contribute to the generation of compositions with artistic value, opening a new chapter in the history of the relationship between chess and technology.

Summary of Research on the Educational Value of Chess presented in the thesis

The specialized literature has consistently highlighted the educational role of strategy games, whose use in teaching has become increasingly common. By integrating them into classroom activities, strategy games can support content consolidation and develop both cognitive and social skills in an attractive and responsible way [56]. Their practice fosters planning, analysis, and decision-making abilities, which are transferable to other domains. Gibson *et al.* [33] show that games can effectively support online learning, provided that their design aligns with learning objectives and is adapted to the students' skills and levels. Technology, they argue, should enhance the learning process but not become an end in itself.

Recent studies confirm the potential of modern games in supporting mathematics education and other subjects. Kebritchi *et al.* [51] demonstrated significant improvements in students' mathematical performance and motivation through the use of educational games, findings that are also supported by [5]. With regard to chess, research emphasizes its extensive academic literature, being noted that more books have been written about chess than about any other game [23], a claim historically supported by Murray [62].

Ferguson [27] synthesized studies showing that chess enhances critical thinking, spatial reasoning, problem-solving, and mathematical skills, while Reyes-Joa *et al.* [68] confirm its role in developing both cognitive skills (strategic thinking, memory, problem-solving) and social ones (rule compliance, collaboration, tolerance to failure). Similarly, Garate-Quispe *et al.* [32] found significant gains in abstract reasoning and school motivation after chess training programs.

Research also compares chess with other types of games. Anderson *et al.* [7] indicate that violent games can increase aggression and reduce empathy, while chess, as a strategic and non-violent game, supports positive educational outcomes. Krebs [76] highlights the potential of serious games to promote ethical decision-making, whereas Trincherro *et al.* [84] and Gliga *et al.* [34] demonstrate that chess enhances abstract reasoning, critical thinking, attention, and school performance.

Nonetheless, some research stresses methodological limitations. Gobet *et al.* [36] and Sala *et al.* [72] argue that findings are sometimes inconclusive or dependent on sample size and study design. Schultetus *et al.* [77] underline the role of memory and position recognition, suggesting that chess expertise cannot be explained solely by calculating optimal moves. The question of knowledge transfer remains open. Franklin [28], also discussed in [48], argued that chess has formative value beyond entertainment, but more recent studies caution that benefits may be limited to the game itself, requiring further research to assess long-term effects across different domains.

In conclusion, most studies confirm the positive effects of chess on cognitive and social development, even though more rigorous research is needed to evaluate the consistency and transferability of these outcomes. In particular, abstract reasoning, memory, and attention have been consistently improved, confirming the educational value of chess and reinforcing its position as a valuable tool for education and cognitive development.

Summary of Research Related to the Security of Strategic Games in the Online Context presented in the thesis

The COVID-19 pandemic had a significant impact on online strategic games, driving their rapid rise in popularity and bringing new concerns regarding data security and digital well-being. In [13], technological solutions are presented showing how 5G networks can enhance player experience while ensuring the protection of personal information. At the same time, Han *et al.* [42] demonstrated that social isolation, anxiety, and intensive use of digital devices have contributed to increased gaming addiction among children and adolescents, emphasizing that prevention efforts should focus on improving social and emotional life, reducing isolation, and promoting a balanced lifestyle.

In this context, the programming of strategic games could include mechanisms such as monitoring playing time, issuing warnings when the duration becomes excessive, mandatory breaks, bonuses for time spent away from the game, and even educational or social mini-games.

A relevant example is chess, whose popularity increased significantly during the pandemic [21]. The transition of competitions to the online environment allowed a much larger global participation but also brought new challenges, such as the risk of players using computer programs to enhance their performance at the expense of fair play. The online experience differs from face-to-face play, affecting skill development, but it enabled the continuation of national and international tournaments despite the cancellation of traditional events. In parallel, strategic games were incorporated into education, fostering critical thinking and social skills [51].

The massive increase in online gaming also amplified vulnerabilities in data protection. According to [13], 5G technology can enable secure collection and management of player data, but Zhao [89] highlights that cybersecurity issues such as attacks and fraud remain frequent, noting that more than 50 countries have already published official strategies in this regard ([89], [55]). Cybersecurity, once primarily associated with protecting critical infrastructures, now extends to the domain of strategic games, where it concerns not only the confidentiality of data but also the fairness of competitions [69].

Fair-play has become a central challenge in online chess. Numerous disqualification cases have demonstrated the need for advanced technological solutions, including artificial intelligence and analytical algorithms capable of distinguishing human-like moves from those generated by external programs ([75], [21], [8]). Although FIDE has issued anti-cheating guidelines, the online environment remains difficult to regulate. Platforms such as Chess.com and Chess24 employ statistical models and machine-learning algorithms to detect improbable moves and protect the integrity of competitions.

Within this framework, the concept of a digital twin [25], [3] has been proposed as an innovative solution for monitoring player behavior by creating a virtual replica and comparing it in real time with actual data. Complementary research on privacy and immersive technologies [66] further highlights both the opportunities and risks of hybrid physical–digital environments.

In conclusion, the pandemic not only accelerated the global popularity of online strategic games but also raised major challenges regarding gaming addiction, data security, and

the preservation of fair play. Technologies such as 5G, artificial intelligence, and digital twin open new pathways for transforming strategic games into a domain with educational, social, and cybersecurity implications.

Summary of the Evolution of Computational Methods used for Chess

This section examines the evolution and diversification of computational methods applied to strategic games, with a special focus on chess, where such approaches have played a central role in advancing artificial intelligence. Beyond position evaluation and the search for optimal moves, computational techniques have been extended to applications such as cheating detection – increasingly necessary in light of the rapid growth of online chess after 2020.

Theoretical foundations include concepts such as decision-making, risk analysis, and resource management. Strategic games rely on decision-tree processes [24], where each choice generates multiple possible branches. Players must evaluate costs and benefits and allocate limited resources efficiently, including time [1]. In chess, these elements are complemented by long-term planning and the use of intuition, which is particularly important under time constraints [35].

The development of search algorithms such as Minimax and Alpha-Beta Pruning marked major steps in optimizing game-tree exploration. Chess became a benchmark for artificial intelligence research as early as the mid-20th century, with a key milestone being Deep Blue’s 1997 victory over world champion Garry Kasparov ([46], [21], [61]). While this achievement relied mainly on brute-force computation, subsequent progress brought a paradigm shift: in 2017, AlphaZero surpassed all existing engines after only four hours of self-learning [80], and in 2019 MuZero advanced further by reaching exceptional performance without being explicitly provided with the rules of the game ([74], [71], [79]). These breakthroughs demonstrated that chess is an ideal testbed for measuring advances in artificial intelligence [2].

Educational applications are equally significant. Strategic games can be used to reinforce knowledge through interactive exercises or mathematical testing [19], while modern platforms such as chess.com foster collaboration, teamwork, and constructive competition [5]. At the same time, scholarship highlights the educational value of chess, which disciplines thinking, improves concentration, and encourages reflection before decision-making [15]. Research by Holding [44] and Gobet [35] emphasizes how chess blends logical reasoning with intuition, making it a powerful tool for cognitive development.

In recent years, debates have also expanded toward artificial creativity. Studies show that artistic productions generated by artificial intelligence can be perceived as indistinguishable from human creations [43], raising questions about originality and authenticity [9], as well as about the redefinition of creativity in an age increasingly shaped by technological systems [60]. The concept of creativity, traditionally considered an exclusively human attribute [16], is now critically reexamined in light of the ability of artificial intelligence to generate outputs that may be perceived as original.

In conclusion, the evolution of computational methods applied to chess – from classical algorithms to advanced systems such as AlphaZero and MuZero – demonstrates the decisive role of strategic games in advancing artificial intelligence. At the same time, the educational potential and the ongoing debates about algorithmic creativity confirm chess as a privileged platform for research, innovation, and the exploration of the intersection between human reasoning and artificial computation.

Different Types of Algorithms Tested with the Help of Strategy Games

Strategic games provide an excellent framework for testing and evaluating algorithms, allowing decision-making under uncertainty and with incomplete information. Artificial intelligence systems have achieved remarkable performance in complex games such as chess and GO ([11], [30], [31], [80], [67]).

Evolutionary algorithms, inspired by the biological metaphor of species adaptation, have proven effective in search and optimization problems where an optimal solution is not required [12]. The early contributions of Box [14], Fraser [29], and Holland [45] laid the foundation for genetic algorithms, later widely applied in artificial intelligence [22]. Although these methods do not guarantee convergence to the optimal solution, several improvements have been proposed for specific contexts [22]. High computational costs and the need for many iterations remain challenges, but technological advances are increasing their efficiency and accessibility.

Machine learning, another key branch of artificial intelligence, also benefits greatly from strategic games, which provide clear rules and objectives. Algorithms can be trained to recognize patterns and develop strategies. Three main approaches are distinguished: feature-based algorithms (with features manually extracted by experts), supervised algorithms (trained on labeled datasets, such as chess diagrams evaluated for aesthetics), and unsupervised algorithms (which discover hidden structures through clustering).

A reference example is MuZero, developed by DeepMind, which combined unsupervised learning with reinforcement learning [74]. In its initial stage, the program played millions of games against itself without labels or explicit rules, autonomously discovering strategic patterns and even original opening variations [71]. By using neural networks and self-play, MuZero achieved superhuman performance, surpassing both elite players and existing engines. These results confirm the extraordinary potential of machine learning in complex games and suggest promising applications in other fields as well [67].

In conclusion, strategic games, due to their complexity and structured nature, have become experimental laboratories for testing and refining evolutionary and machine learning algorithms, decisively contributing to the progress of artificial intelligence.

Possible Directions of Technological Development in the Context of Strategy Games

Strategic games have proven to be a fertile ground for exploring computational methods, with applications extending beyond the gaming industry into education and research [58]. Modern techniques such as machine learning, neural networks, augmented reality (AR), and virtual reality (VR) have opened new perspectives in the educational field. Augmented reality enables the integration of digital elements into the real world, while virtual reality creates immersive environments with applications ranging from scientific explorations to historical contexts. Recent studies highlight the educational potential of these technologies; Yu *et al.* [88], through a meta-analysis of 43 studies, emphasized the positive impact of virtual reality on learning, with the exception of primary education.

In chess-related research, the use of a digital twin architecture was proposed in [3], where the MyMLTwin model integrates machine learning and deep learning algorithms. This approach allows the evaluation of chess compositions according to criteria such as originality and complexity, offering objective assessments and detailed feedback, adaptable to community standards. Thus, digital twins not only support chess but also contribute to technological progress in a reciprocal manner [21].

At the same time, the proliferation of artificial intelligence tools has sparked pedagogical and ethical debates. Some studies have raised concerns about a potential decline in critical thinking [81], while others have discussed whether such tools should be restricted in academia [37], [87]. On the other hand, generative applications such as ChatGPT can be constructively integrated into education [5]. The emergence of these systems has triggered discussions about creativity ([60], [86]), the labor market ([54], [63], [6]), and legal issues including copyright [41], [73].

Creativity, defined as the ability to generate ideas that are both novel and useful ([39], [70]), is linked to cognitive flexibility [17] and to associative theory [59], supported by computational studies [52] and brain imaging research [65]. The incursion of artificial intelligence into the arts has resulted in high-quality works [64], though critics argue these may lack authentic originality [57]. Nonetheless, recent research suggests that artificial intelligence may achieve levels of creativity comparable to human output [40].

In conclusion, computational methods and emerging technologies – from augmented reality and virtual reality to digital twins and generative artificial intelligence – have transformed the role of strategic games, including chess, into platforms for testing and innovation. They confirm the central role of these games in technological progress and open new horizons for education and creativity.

Research Conclusions

In this thesis, it was examined the progress of computational methods in the context of strategic games and explored their implications for the future of artificial intelligence. For example, advances in computational techniques used by chess engines have paved the way for numerous improvements in artificial intelligence. Strategic games have long been a subject of interest for AI researchers. One of the main reasons is that these games offer a perfect environment for testing and improving various artificial intelligence techniques and algorithms. Strategic games have played a significant role in technological progress, particularly in the development of AI algorithms. Chess, as well as other strategy games, has been used as a benchmark for developing and testing artificial intelligence algorithms [26]. These games have helped researchers understand both the limitations and the capabilities of AI algorithms and have led to substantial advancements in machine learning, neural networks, and related fields. Computational methods have been applied to strategic games to analyze complex strategies, optimize decision-making processes, and create game-playing agents capable of defeating human experts. Chess is one of the most extensively studied strategic games in this regard.

The use of strategic games in education has also been a significant topic of interest. In [5], I proposed approaches that combine various learning techniques, including the teaching of strategic games such as chess, with the aim of analyzing and improving educational processes.

Studies have shown that practicing strategic games can offer numerous benefits for cognitive development, including improved memory, problem-solving skills, and spatial reasoning. Strategic games may also enhance social skills such as teamwork, communication, and sportsmanship. Moreover, chess has been used as a teaching tool for subjects such as mathematics and has been integrated into school and university curricula in many countries. Research on the educational benefits of chess has attracted considerable interest in recent decades. A variety of studies have examined the impact of chess on children's cognitive and educational development. Many researchers argue that chess may offer benefits for strategic thinking, decision-making, problem-solving, and the development of mathematical abilities. Chess requires anticipation, evaluation of consequences, and adaptation to change, all of which can strengthen strategic thinking. Therefore, chess has been considered a valuable tool for improving problem-solving skills, as players must identify and apply strategies to overcome obstacles during the game. Regarding decision-making, some research suggests that chess may improve the ability to evaluate options, anticipate outcomes, and make informed decisions, and that these skills may transfer to other contexts in real life, supporting effective learning and decision-making. Additionally, several studies indicate that practicing chess may contribute to the development of mathematical skills, proposing that the problem-solving abilities required in chess may transfer to mathematics, supporting the understanding of mathematical concepts and the solving of complex mathematical problems ([34], [84]).

This doctoral work sought to investigate the role of strategic games in the development and testing of artificial intelligence algorithms. Throughout the research, I showed that strategic games have been an important reference point in the development and testing of AI algorithms for several decades. Their importance within AI research was also analyzed, and the findings indicate that strategic games have played a significant role in recent advances in machine learning, deep neural networks, and related domains. Another major

objective of the research was to analyze the impact of strategic games on the development of new AI algorithms and their application in various fields. The results show that strategic games can be a valuable tool in developing new artificial intelligence algorithms and in applying these algorithms across diverse areas. The analysis of the potential of strategic games as an instrument for enhancing cognitive abilities in education was also one of the objectives. It was found that strategic games can be successfully used in educational contexts to improve students' cognitive skills.

Regarding the analysis of factors that significantly influence the value of a composed chess diagram, the research focused on designing an algorithm capable of generating and evaluating chess diagrams automatically. The ability to automatically evaluate chess diagrams would represent a significant breakthrough in both gaming and artificial intelligence. As shown in Chapter 4, through precise formulations we can define and automatically verify the presence of certain “beauty” criteria in chess compositions. These definitions enabled the implementation of automatic verification algorithms for the stated criteria, including the detection of themes present in diagrams, thus facilitating the analysis and appreciation of chess problems. Furthermore, by analyzing the strategies and techniques used by the algorithm to generate diagrams and their solutions, it becomes possible to gain insights into the thought processes and decision-making strategies used by human composers ([18], [10]). This may lead to a better understanding of the fundamental principles of chess composition and contribute to the development of new techniques and strategies. Thus, the process of automatically composing chess diagrams has the potential to revolutionize the field of chess composition.

The final step will be writing a book containing the automatically composed chess diagrams and their likewise automatically generated solutions. The book will be organized beginning with diagrams containing fewer pieces and gradually increasing the level of complexity, up to more sophisticated compositions featuring diverse themes.

Due to its complex but well-defined nature, chess has proven to be a perfect environment for testing machine learning algorithms and for evaluating progress in artificial intelligence [26]. It is important to highlight that, although the results may appear similar—both Deep Blue and Google's AlphaZero managed to play chess more strongly than any human—the processes used to achieve these results were entirely different. Google DeepMind's AlphaZero learning process emulated “human-like” learning. To clarify this distinction, consider the following example: If we design a robot's software to answer a question in a particular way merely because it happens to be one of the million question-answer pairs stored in a database, this is brute force. But designing a robot's software to “learn” how to answer any question based on the conversations available on the internet—similar to the way humans learn through observation, interaction with the environment, and imitation—so that it becomes capable of formulating a response to any question, is a completely different process. Even if the outcome might be the same, such as replying “I'm fine, thank you!” to the question “How are you feeling?”, the underlying mechanism is fundamentally distinct.

Bibliographic References

- [1] Bruce Abramson. “Control strategies for two-player games”. In: *ACM Comput. Surv.* 21.2 (1989), pp. 137–161. ISSN: 0360-0300. DOI: 10.1145/66443.66444. URL: <https://doi.org/10.1145/66443.66444>.
- [2] Ajay Agrawal, Joshua S. Gans, and Avi Goldfarb. “Exploring the impact of artificial Intelligence: Prediction versus judgment”. In: *Information Economics and Policy* 47 (2019). The Economics of Artificial Intelligence and Machine Learning, pp. 1–6. ISSN: 0167-6245. DOI: 10.1016/j.infoecopol.2019.05.001.
- [3] Constantin Lucian Aldea, Razvan Bocu, and Delia Monica Duca Iliescu. “Health Parameters Monitoring Through an Integrated Multilayer Digital Twin Architecture”. In: *Advanced Information Networking and Applications (AINA)*. Ed. by Leonard Barolli. Cham: Springer Nature Switzerland, 2024, pp. 298–309. ISBN: 978-3-031-57840-3. URL: https://link.springer.com/chapter/10.1007/978-3-031-57840-3_27.
- [4] Constantin Lucian Aldea, Razvan Bocu, and Delia Monica Duca Iliescu. “On the analysis and prediction of chess diagram scores using artificial neural networks”. In: *The 40-th International Conference on Advanced Information Networking and Applications (AINA), 2026*.
- [5] Constantin Lucian Aldea et al. “Efficient Didactic Methods Used in Modern E-Learning and Traditional Environments”. In: *Information and Software Technologies*. Springer Nature Switzerland, 2025, pp. 266–280. ISBN: 978-3-031-84263-4. DOI: 10.1007/978-3-031-84263-4_22. URL: https://link.springer.com/chapter/10.1007/978-3-031-84263-4_22.
- [6] Nantheera Anantrasirichai and David Bull. “Artificial intelligence in the creative industries: a review”. In: *Artif. Intell. Rev.* 55.1 (2022), pp. 589–656. DOI: 10.1016/j.chb.2023.107707.
- [7] Craig Anderson et al. “Violent video game effects on aggression, empathy, and prosocial behavior in eastern and western countries: a meta-analytic review”. en. In: *Psychol. Bull.* 136.2 (2010), pp. 151–173.
- [8] Jo~ao Batista Andrade et al. “Analysis of cheating in human patterns using Stockfish suggestions”. In: *XXIII Simposio Brasileiro de Jogos e Entretenimento Digital (SBGames 2024)*. 2024. DOI: https://doi.org/10.5753/sbgames_estendido.2024.241054. eprint: https://sol.sbc.org.br/index.php/sbgames_estendido/article/view/31999/31801.
- [9] Leonardo Arriagada. “CG-Art: demystifying the anthropocentric bias of artistic creativity”. In: *Connection Science* 32.4 (2020), pp. 398–405. DOI: 10.1080/09540091.2020.1741514.

- [10] Susan C. Athey, Kevin A. Bryan, and Joshua S. Gans. “The Allocation of Decision Authority to Human and Artificial Intelligence”. In: *AEA Papers and Proceedings* 110.None (2020), pp. 80–84. DOI: 10.1257/pandp.20201034. URL: <https://ideas.repec.org/a/aea/apandp/v110y2020p80-84.html>.
- [11] Werner Binder. “AlphaGo’s Deep Play: Technological Breakthrough as Social Drama”. In: Palgrave Macmillan, Jan. 2021, pp. 167–195. ISBN: 978-3-030-56285-4. DOI: 10.1007/978-3-030-56286-1_6.
- [12] Dorin Bocu. *Conceptual si aplicativ in programarea logica si functionala*. Editura Matrix Rom, 2020. ISBN: 9786062505882.
- [13] Razvan Bocu, Anca Vasilescu, and Delia Monica Duca Iliescu. “Personal Health Metrics Data Management Using Symmetric 5G Data Channels”. In: *Symmetry* 14.7 (2022). ISSN: 2073-8994. DOI: 10.3390/sym14071387.
- [14] George E. P. Box. “Evolutionary Operation: a Method for Increasing Industrial Productivity”. In: *Journal of The Royal Statistical Society Series C-applied Statistics* 6 (1957), pp. 81–101. DOI: 10.2307/2985505.
- [15] Pius Brînzeu. *Șahul – Magie în alb și negru*. Editura de Vest, 1995. ISBN: 973-36-0250-7.
- [16] Rebecca Chamberlain et al. “Putting the art in artificial: Aesthetic responses to computer-generated art.” In: *Psychology of Aesthetics, Creativity, and the Arts* 12 (2017), p. 177. DOI: 10.1037/aca0000136.
- [17] Sun Hee Cho et al. “The Relationship Between Diverse Components of Intelligence and Creativity”. In: *The Journal of Creative Behavior* 44 (2010). DOI: 10.1002/j.2162-6057.2010.tb01329.x.
- [18] Sukwoong Choi et al. “How Does AI Improve Human Decision-Making? Evidence from the AI-Powered Go Program”. In: *SSRN Electronic Journal* (July 2021). DOI: 10.2139/ssrn.3893835.
- [19] Opeyemi Dele-Ajayi et al. “Learning mathematics through serious games: An engagement framework”. In: *2016 IEEE Frontiers in Education Conference (FIE)*. 2016, pp. 1–5. DOI: 10.1109/FIE.2016.7757401. URL: <https://ieeexplore.ieee.org/document/7757401>.
- [20] Emilian Dobrescu. “The Chess Study as a Multi-criteria System”. In: *EG* 123 (1997), pp. 30–47. eprint: https://www.arves.org/arves/images/PDF/EG_PDF/eg123.pdf.
- [21] Delia Monica Duca Iliescu. “The Impact of Artificial Intelligence on the Chess World”. In: *JMIR Serious Games* 8.4 (2020), e24049. ISSN: 2291-9279. DOI: 10.2196/24049. URL: <http://games.jmir.org/2020/4/e24049/>.
- [22] D Dumitrescu. *Algoritmi genetici și strategii evolutive: aplicații în Inteligența Artificială și în domenii conexe*. Editura Albastră, 2019.
- [23] James Eade and AL Lawrence. *Biblia jucătorului de șah: strategii ilustrate pentru a fi mereu în avantaj*. Didactica Publishing House (DPH), 2021. URL: <https://www.edituradph.ro/biblia-jucatorului-de-sah-strategii-ilustrate-pentru-a-fi-mereu-in-avantaj.html>.
- [24] Ahmed A. Elnaggar et al. “A Comparative Study of Game Tree Searching Methods”. In: *International Journal of Advanced Computer Science and Applications* 5.5 (2014). DOI: 10.14569/IJACSA.2014.050510. URL: <http://dx.doi.org/10.14569/IJACSA.2014.050510>.

- [25] Philip Empl et al. “Digital Twins in Security Operations: State of the Art and Future Perspectives”. In: *ACM Comput. Surv.* 58.1 (2025). ISSN: 0360-0300. DOI: 10.1145/3746279. URL: <https://doi.org/10.1145/3746279>.
- [26] Nathan Ensmenger. “Is chess the drosophila of artificial intelligence? A social history of an algorithm”. In: *Social Studies of Science* 42.1 (2012). PMID: 22530382, pp. 5–30. DOI: 10.1177/0306312711424596. URL: <https://journals.sagepub.com/doi/abs/10.1177/0306312711424596>.
- [27] Robert Ferguson. *Chess in Education Research Summary*. <https://www.scholasticchess.mb.ca/docs/ciers.pdf>. Accessed: 2025-09-01. 1995.
- [28] Benjamin Franklin. “The Morals of Chess. *Columbian Magazine*, 1786”. In: *Columbian Magazine* (1786).
- [29] Alex Fraser. “Simulation of Genetic Systems by Automatic Digital Computers I. Introduction”. In: *Australian Journal of Biological Sciences* 10 (1957), pp. 484–491. DOI: 10.1071/BI9570484.
- [30] Yifan Gao. “PGD: A Large-scale Professional Go Dataset for Data-driven Analytics”. In: *2022 IEEE Conference on Games (CoG)*. 2022, pp. 284–291. DOI: 10.1109/CoG51982.2022.9893704.
- [31] Yifan Gao, Danni Zhang, and Haoyue Li. “The Professional Go Annotation Dataset”. In: *IEEE Transactions on Games PP* (2023), pp. 1–10. DOI: 10.1109/TG.2023.3275183.
- [32] Jorge Santiago Garate-Quispe et al. “Effect of chess teaching on mathematical, attention and concentration abilities in school-aged children of the Peruvian Amazon”. In: *Apuntes Universitarios* 11.1 (2020), pp. 1–22. DOI: 10.17162/au.v11i1.542. eprint: <https://apuntesuniversitarios.upeu.edu.pe/index.php/revapuntes/article/view/542/628>. URL: <https://apuntesuniversitarios.upeu.edu.pe/index.php/revapuntes/article/view/542>.
- [33] David Gibson, Clark Aldrich, and Marc Prensky. *Games and Simulations in Online Learning: Research and Development Frameworks*. IGI Global Scientific Publishing, 2006. ISBN: 9781599043043. DOI: 10.4018/978-1-59904-304-3.
- [34] Fotinica Gliga and Petru Iulian Flesner. “Cognitive Benefits of Chess Training in Novice Children”. In: *Procedia - Social and Behavioral Sciences* 116 (2014). 5th World Conference on Educational Sciences, pp. 962–967. ISSN: 1877-0428. DOI: 10.1016/j.sbspro.2014.01.328. URL: <https://www.sciencedirect.com/science/article/pii/S1877042814003450>.
- [35] Fernand Gobet. *The Psychology of Chess*. Sept. 2018. ISBN: 9781315441887. DOI: 10.4324/9781315441887.
- [36] Fernand Gobet and Guillermo Campitelli. “Educational benefits of chess instruction: A critical review”. In: University of Texas. Chess Program, 2006, pp. 124–143. ISBN: 978-0-9786742-0-5. eprint: <https://researchportal.murdoch.edu.au/esploro/outputs/bookChapter/Educational-benefits-of-chess-instruction-A/991005542720507891/filesAndLinks?index=0>. URL: <https://researchportal.murdoch.edu.au/esploro/outputs/bookChapter/Educational-benefits-of-chess-instruction-A/991005542720507891>.
- [37] Simone Grassini. “Shaping the Future of Education: Exploring the Potential and Consequences of AI and ChatGPT in Educational Settings”. In: *Education Sciences* (2023). DOI: 10.3390/educsci13070692. URL: <https://www.mdpi.com/2227-7102/13/7/692>.

- [38] Simone Grassini and Mika Koivisto. “Artificial Creativity? Evaluating AI Against Human Performance in Creative Interpretation of Visual Stimuli”. In: *International Journal of Human–Computer Interaction* 41.7 (2025), pp. 4037–4048. DOI: 10.1080/10447318.2024.2345430. eprint: <https://www.tandfonline.com/doi/epdf/10.1080/10447318.2024.2345430?needAccess=true>.
- [39] J Paul Guilford. “Creativity: Yesterday, Today and Tomorrow”. In: *Journal of Creative Behavior* 1 (1967), pp. 3–14. DOI: 10.1002/j.2162-6057.1967.tb00002.x.
- [40] Jennifer Haase and Paul Hanel. “Artificial muses: Generative Artificial Intelligence Chatbots Have Risen to Human-Level Creativity”. In: *Journal of Creativity* 33 (2023). DOI: 10.48550/arXiv.2303.12003.
- [41] Philipp Hacker. “A legal framework for AI training data—from first principles to the Artificial Intelligence Act”. In: *Law, Innovation and Technology* 13.2 (2021), pp. 257–301. DOI: 10.1080/17579961.2021.1977219.
- [42] Tae Sun Han et al. “A systematic review of the impact of COVID-19 on the game addiction of children and adolescents”. In: *Front. Psychiatry* 13 (2022), p. 976601.
- [43] Jimpei Hitsuwari et al. “Does human–AI collaboration lead to more creative art? Aesthetic evaluation of human-made and AI-generated haiku poetry”. In: *Comput. Hum. Behav.* 139.C (2023). ISSN: 0747-5632. DOI: 10.1016/j.chb.2022.107502. URL: <https://doi.org/10.1016/j.chb.2022.107502>.
- [44] D.H. Holding. *The Psychology of Chess Skill*. Psychology Revivals. Taylor & Francis, 2021. ISBN: 9781000394658. URL: <https://books.google.ro/books?id=JG8IEQAAQB AJ>.
- [45] J.H. Holland. *Adaptation in Natural and Artificial Systems: An Introductory Analysis with Applications to Biology, Control, and Artificial Intelligence*. University of Michigan Press, 1975. ISBN: 9780472084609. URL: <https://books.google.ro/books?id=JE5RAAAAMAAJ>.
- [46] Feng-Hsiung Hsu. *Behind Deep Blue: Building the Computer that Defeated the World Chess Champion*. Princeton University Press, 2002. ISBN: 9780691090658.
- [47] Anatole Ianovcic. *Şahul Artistic*. Editura Sport-Turism, 1979. URL: https://archive.org/details/ianovcic-anatole-f.-sahul-artistic-scan_202408.
- [48] Bogdan Ionescu. *Morala Şahului*. Editura Neverland, 2022. URL: <https://www.neverland.ro/carte/morala-ahului-2/>.
- [49] Azlan Iqbal. “Evaluation of Economy in a Zero-sum Perfect Information Game”. In: *The Computer Journal* 51.4 (2007), pp. 408–418. ISSN: 0010-4620. DOI: 10.1093/comjnl/bxm060.
- [50] Lavesh Nama Kamalesh. “Chess Puzzle Generation using Stockfish and Genetic Algorithms”. In: *International Journal of Scientific Research and Engineering Development* 6.2 (2023). Articol open access; generare de puzzle-şah cu algoritmi genetici şi Stockfish, pp. 1458–1465. URL: <https://ijsred.com/volume6/issue2/IJSRED-V6I2 P182.pdf>.
- [51] Mansureh Kebritchi, Atsusi Hirumi, and Haiyan Bai. “The effects of modern mathematics computer games on mathematics achievement and class motivation”. In: *Computers and Education* 55.2 (2010), pp. 427–443. ISSN: 0360-1315. DOI: <https://doi.org/10.1016/j.compedu.2010.02.007>. URL: <https://www.sciencedirect.com/science/article/pii/S0360131510000412>.

- [52] Yoed N. Kenett and Miriam Faust. “A Semantic Network Cartography of the Creative Mind”. In: *Trends in Cognitive Sciences* 23 (2019), pp. 271–274. URL: [10.1016/j.tics.2019.01.007](https://doi.org/10.1016/j.tics.2019.01.007).
- [53] Mohd Nor Akmal Khalid. “Ludogenic innovation: How playing incentivizes technological innovation”. In: *Entertainment Computing* 52 (2025), p. 100900. ISSN: 1875-9521. DOI: <https://doi.org/10.1016/j.entcom.2024.100900>. URL: <https://www.sciencedirect.com/science/article/pii/S1875952124002684>.
- [54] Dong Hwa Kim. “A Study on the Job Replacement Impact of ChatGPT and Education Method”. In: *European Journal of Science, Innovation and Technology* 3.4 (2023), pp. 105–122. URL: <https://ejst-journal.com/index.php/ejst/article/view/245>.
- [55] Alexander Klimburg. *National Cyber Security Framework Manual*. NATO CCD COE Publications, 2012. ISBN: 978-9949-9211-1-9.
- [56] Sagrario Lantarón et al. “Improving the Teaching of Real Valued Functions Using Serious Games. Binary Who Is Who?” In: *Mathematics* 9.11 (2021). ISSN: 2227-7390. DOI: [10.3390/math9111239](https://doi.org/10.3390/math9111239). URL: <https://www.mdpi.com/2227-7390/9/11/1239>.
- [57] Edward Lee. “Digital Originality”. In: *anderbilt Journal of Entertainment and Technology Law* 14 (2020), p. 919. eprint: https://scholarship.kentlaw.iit.edu/cgi/viewcontent.cgi?article=1351&context=fac_schol. URL: <https://ssrn.com/abstract=2128799>.
- [58] Robert Levinson et al. “The Role of Chess in Artificial Intelligence Research”. In: *ICGA Journal* 14.3 (1991), pp. 153–161. DOI: [10.3233/ICG-1991-14314](https://doi.org/10.3233/ICG-1991-14314). eprint: <https://journals.sagepub.com/doi/pdf/10.3233/ICG-1991-14314>. URL: <https://journals.sagepub.com/doi/abs/10.3233/ICG-1991-14314>.
- [59] Sarnoff Mednick. “The Associative Basis of the Creative Process”. In: *Psychological review* 69 (1962), pp. 220–32. DOI: [10.1037/h0048850](https://doi.org/10.1037/h0048850).
- [60] Kobe Millet et al. “Defending humankind: Anthropocentric bias in the appreciation of AI art”. In: *Computers in Human Behavior* 143 (2023), p. 107707. ISSN: 0747-5632. DOI: <https://doi.org/10.1016/j.chb.2023.107707>. URL: <https://www.sciencedirect.com/science/article/pii/S0747563223000584>.
- [61] Karsten Müller and Jonathan Schaeffer. *Man vs. Machine Challenging Human Supremacy at Chess*. Russell Enterprises, 2022. URL: <https://www.russell-enterprises.com/russell-enterprises/man-vs-machinebrchallenging-human-supremacy-a-t-chess>.
- [62] H. J. R. Murray. *A History of Chess*. Oxford: Oxford University Press, 1913.
- [63] Trinh Nguyen and Amany Elbanna. “Understanding Human-AI Augmentation in the Workplace: A Review and a Future Research Agenda”. In: *Information Systems Frontiers* (Mar. 2025), pp. 1–21. DOI: [10.1007/s10796-025-10591-5](https://doi.org/10.1007/s10796-025-10591-5).
- [64] Atte Oksanen et al. “Artificial intelligence in fine arts: A systematic review of empirical research”. In: *Computers in Human Behavior: Artificial Humans* 1.2 (2023), p. 100004. ISSN: 2949-8821. DOI: <https://doi.org/10.1016/j.chbah.2023.100004>.
- [65] Marcela Ovando-Tellez et al. “Brain connectivity-based prediction of real-life creativity is mediated by semantic memory structure”. In: *Science Advances* 8.5 (2022), eabl4294. DOI: [10.1126/sciadv.abl4294](https://doi.org/10.1126/sciadv.abl4294). eprint: <https://www.science.org/doi/pdf/10.1126/sciadv.abl4294>. URL: <https://www.science.org/doi/abs/10.1126/sciadv.abl4294>.

- [66] Carolina Pereira et al. “Security and Privacy in Physical–Digital Environments: Trends and Opportunities”. In: *Future Internet* 17.2 (2025), p. 83. DOI: 10.3390/fi17020083. URL: <https://www.mdpi.com/1999-5903/17/2/83>.
- [67] Dale Purves. “Opinion: What does AI’s success playing complex board games tell brain scientists?” In: *Proceedings of the National Academy of Sciences* 116 (2019), pp. 14785–14787. DOI: 10.1073/pnas.1909565116. eprint: <https://www.pnas.org/doi/full/10.1073/pnas.1909565116>.
- [68] Haydee María Reyes-Joa, Darvin Manuel Ramírez-Guerra, and Lázaro Antonio Bueno-Pérez. “El ajedrez y la rehabilitación. The chess and the rehabilitation”. In: *Arrancada* 20.37 (2020), pp. 201–220. eprint: <https://revistarrancada.cujae.edu.cu/index.php/arrancada/article/view/335/237>. URL: <https://revistarrancada.cujae.edu.cu/index.php/arrancada/article/view/335>.
- [69] Basheer Riskhan. “Physical Security to Cybersecurity (Challenges and Implications in the Modern Digital Landscape)”. In: *Journal of Electrical Systems* 20 (Apr. 2024), pp. 692–702. DOI: 10.52783/jes.2090.
- [70] Mark Runco and Garrett Jaeger. “The Standard Definition of Creativity”. In: *Creativity Research Journal - CREATIVITY RES J* 24 (Jan. 2012), pp. 92–96. DOI: 10.1080/10400419.2012.650092.
- [71] Matthew Sadler and Natasha Regan. *Game Changer: AlphaZero’s Groundbreaking Chess Strategies and the Promise of AI*. Continental Sales, Incorporated, 2019. ISBN: 9789056918231. URL: <https://books.google.ro/books?id=U4CFDwAAQBAJ>.
- [72] Giovanni Sala and Fernand Gobet. “Do the benefits of chess instruction transfer to academic and cognitive skills? A meta-analysis”. In: *Educational Research Review* 18 (2016), pp. 46–57. ISSN: 1747-938X. DOI: <https://doi.org/10.1016/j.edurev.2016.02.002>. URL: <https://www.sciencedirect.com/science/article/pii/S1747938X16300112>.
- [73] Pamela Samuelson. “Generative AI meets copyright”. In: *Science* 381.6654 (2023), pp. 158–161. DOI: 10.1126/science.adi0656. eprint: <https://www.science.org/doi/pdf/10.1126/science.adi0656>. URL: <https://www.science.org/doi/abs/10.1126/science.adi0656>.
- [74] Julian Schrittwieser et al. “Mastering Atari, Go, chess and shogi by planning with a learned model”. In: *Nature* 588.7839 (2020), pp. 604–609. ISSN: 1476-4687. DOI: 10.1038/s41586-020-03051-4. URL: <https://doi.org/10.1038/s41586-020-03051-4>.
- [75] Kim Schu and Nils Haller. “Cheating and Doping in Chess – A Survey among 1,924 German Club Players using the Randomized Response Technique”. In: *Performance Enhancement & Health* 13.3 (2025), p. 100344. ISSN: 2211-2669. DOI: <https://doi.org/10.1016/j.peh.2025.100344>.
- [76] Jacqueline Schuldt née Krebs. “Moral Dilemmas in Serious Games”. In: 2013. DOI: 10.2991/icaicte.2013.46.
- [77] Richard S. Schultetus and Neil Charness. “Recall or Evaluation of Chess Positions Revisited: The Relationship between Memory and Evaluation in Chess Skill”. In: *The American Journal of Psychology* 112.4 (1999), pp. 555–569. ISSN: 00029556. DOI: 10.2307/1423650. URL: <http://www.jstor.org/stable/1423650>.
- [78] Claude E. Shannon. “Programming a Computer for Playing Chess”. In: *Computer Chess Compendium*. Ed. by David Levy. New York, NY: Springer New York, 1988, pp. 2–13. ISBN: 978-1-4757-1968-0. DOI: 10.1007/978-1-4757-1968-0_1. URL: https://doi.org/10.1007/978-1-4757-1968-0_1.

- [79] David Silver et al. “A general reinforcement learning algorithm that masters chess, shogi, and Go through self-play”. In: *Science* 362.6419 (2018), pp. 1140–1144. DOI: 10.1126/science.aar6404. eprint: <https://www.science.org/doi/pdf/10.1126/science.aar6404>. URL: <https://www.science.org/doi/abs/10.1126/science.aar6404>.
- [80] David Silver et al. *Mastering Chess and Shogi by Self-Play with a General Reinforcement Learning Algorithm*. Dec. 2017. DOI: 10.48550/arXiv.1712.01815.
- [81] Jonathan Michael Spector and Shanshan Ma. “Inquiry and critical thinking skills for the next generation: from artificial intelligence back to human intelligence”. In: *Smart Learning Environments* 6.1 (2019). DOI: 10.1186/s40561-019-0088-z.
- [82] Simon Stoiljkovikj, Ivan Bratko, and Matej Guid. “A Computational Model for Estimating the Difficulty of Chess Problems”. In: *Proceedings of the Third Annual Conference on Advances in Cognitive Systems*. 2015. eprint: <http://www.cogsys.org/proceedings/2015/paper-2015-7.pdf>.
- [83] A. Toth. *Exploration in Chess Beauty*. Andras Toth, 2012. URL: <https://books.google.ro/books?id=kYf0MgEACAAJ>.
- [84] Roberto Trinchero and Giovanni Sala. “Chess training and mathematical problem-solving: The role of teaching heuristics in transfer of learning.” In: *Eurasia Journal of Mathematics, Science & Technology Education* 12.3 (2016), pp. 655–668. DOI: 10.12973/eurasia.2016.1255a. eprint: <https://www.ejmste.com/download/chess-training-and-mathematical-problem-solving-the-role-of-teaching-heuristics-in-transfer-of-4483.pdf>. URL: <https://doi.org/10.12973/eurasia.2016.1255a>.
- [85] M Velimirovic and K Valtonen. *The definitive book. Encyclopedia of Chess Problems: Themes and Terms*. Chess Informant, 2020. URL: <https://sahovski.com/ENCYCLOPAEDIA-OF-CHESS-PROBLEMS-Themes-and-Terms-p114360268>.
- [86] Ryan Watkins and Eran Barak-Medina. “AI’s Influence on Human Creative Agency”. In: *Creativity Research Journal* (2024), pp. 1–13. DOI: 10.1080/10400419.2024.2437264.
- [87] Hao Yu. “Reflection on whether Chat GPT should be banned by academia from the perspective of education and teaching”. In: *Frontiers in Psychology* 14 (2023), p. 1181712. DOI: 10.3389/fpsyg.2023.1181712.
- [88] Zhonggen Yu and Wei Xu. “A meta-analysis and systematic review of the effect of virtual reality technology on users’ learning outcomes”. In: *Computer Applications in Engineering Education* 30 (2022). DOI: 10.1002/cae.22532.
- [89] Chen Zhao. “Cyber security issues in online games”. In: *Proceedings of the 2nd International Conference on Advances in Materials, Machinery, Electronics (AMME 2018)*. Vol. 1955. 2018, p. 040015. DOI: 10.1063/1.5033679.